

GEOTECHNICAL REPORT

West Mountain Road over Kitchen Brook
Culvert Strengthening
C-10-024
February 2025
Cheshire, Massachusetts

Prepared for:

Town of Cheshire



Gill Engineering Associates, Inc.
63 Kendrick Street
Needham, MA 02494



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1. INTRODUCTION

1.1. Scope of Report

The purpose of this report is to summarize the geotechnical findings from the subsurface investigation and to provide recommendations for the reuse of the existing footings and the proposed wingwalls as part of the C-10-024 (AB2) culvert strengthening project in the Town of Cheshire, Massachusetts. The culvert strengthening is necessary due to the poor condition of the existing culvert. This report will evaluate the data from the subsurface exploration and provide the necessary parameters for designing the proposed wingwalls. All parameters provided will be in accordance with AASHTO LRFD 9th Edition Design Specifications and the 2024 LRFD MassDOT Bridge Manual. The report will also provide recommendations for the construction of the proposed wingwalls with guidance on minimizing potential construction issues.

1.2. Existing Structure and Site History

Bridge C-10-024 (AB2) is located on West Mountain Road and spans over Kitchen Brook as illustrated in Appendix 6.1 – Project Locus Map. The existing bridge is a corrugated steel arch with an open bottom on concrete footings. The clear opening of the existing culvert is 15'-8"± and the total length of the culvert is 42'-7"±.

The south headwall of the culvert has areas of settled stones, with the east half displaced up to 24". The corrugated pipe has areas of minor rusting with delamination and active leakage along the footings, with the entire arch rusted at the south end. The concrete footings are exposed up to 5-feet on either side. Both footings have a vertical crack above the utility box with a spall at the top of the east footing crack. There is localized scour on the downstream side (south end) of the utility box. At the southeast embankment there is a disconnected drain pipe causing moderate erosion. The wearing surface has several cracks and patches. There is minor collision damage to the southwest guardrail terminal end and last panel.

1.3. Site Description

West Mountain Road is oriented west-to-east and provides a single lane of traffic in either direction. It is classified as a Rural Local Road with an ADT of 350 as of 2020. The bridge location is surrounded by residential homes and some trees and vegetation. There is an underground utility vault located at the northwest corner of the project site that provides access to the 8" water main that runs along West Mountain Road.

At the project site, Kitchen Brook is lain with sandy soil and cobble stones. The slopes upstream and downstream of the bridge contain debris and are overgrown with low lying heavy vegetation. The stream site drainage area mostly consists of forest and grassland with some residential development.

2. SUBSURFACE CONDITIONS

2.1. Local Geology

According to the geologic map of the Cheshire quadrangle, the site geology contains a mix of sand, some silt, some clay with pebbles, cobble, boulder clasts, and some large surface boulders. The area has shallow bedrock with till generally less than 10 to 15 feet thick. See Appendix 6.2 for the map.

2.2. Subsurface Exploration

The subsurface exploration consisted of two (2) soil borings located just offset from the end of the existing culvert at both approaches (designated as B-1 and B-2). The borings were drilled using a 3 1/4-inch casing and a 1 3/8-inch split spoon sampler on September 25, 2023 and September 26, 2023 by New England Boring Contractors, Inc. of Derry, New Hampshire and observed by Gill Engineering Associates, Inc. (GEA) which included a visual and hands-on examination of the soil samples. See Appendix 6.3 for an as-drilled boring site plan and Appendix 6.4 for boring logs. GEA has prepared the boring logs presented in this report.

2.3. Subsurface Profile

2.3.1. East Boring B-1

The existing ground grade at B-1 is at 1122.9. The top 3 feet consist of dry, light brown-grey medium dense fine sand with some coarse sand. The layer from 5 feet to 7 feet consists of moist, light grey loose sand with some fine gravel. The layer below to 12 feet consists of moist, grey medium dense sand with fine and coarse gravel. The layer from 15 to 17 feet consists of wet, grey dense to very dense sand with gravel and traces of clay. The final layer from 20 feet to 22 feet consists of wet, grey silty-clay with some fine cobbles and coarse gravel. Refusal was met at a depth of 25 feet. Overall, the top 12 feet consists of medium dense granular material with SPT blow counts in the range of 10-30. Below 12 feet consists of very dense granular material with SPT blow counts exceeding 50. Bedrock was encountered at a depth of 28 feet.

2.3.2. West Boring B-2

The existing ground grade at B-2 is 1123.2. The top 3 feet consist of dry, loose to medium dense brown sand. The layer from 5 to 7 feet consists of moist, loose dark grey sand. The layer below to 12 feet consists of moist, medium dense dark grey sand with some fine cobbles. The layer from 15 to 17 feet consists of wet, brown-tan medium dense sand and stiff clay with traces of coarse sand. The next layer to 22 feet consists of wet, brown-tan medium to very stiff clay and medium dense fine sand. The final layer from 25 feet to 27 feet consists of wet, brown-tan with layers of light grey

very stiff clay with traces of medium dense sand. A rock core was then taken at a depth of 30 feet. Overall, the top 12 feet consists of medium dense granular material with SPT blow counts in the range of 10-30. Below 12 feet consists of hard clay material with SPT blow counts exceeding 30.

2.3.3. Soil Testing

Due to the field identification of clay material within the depth of boring B-2, three separate samples were sent out for testing to determine the Atterberg Limits of the material. Samples S4, S5, and S6, with depths ranging from 15'-27' deep were tested. Refer to Appendix 6.5 for testing results. Generally, the samples were found to have relatively high consistency indexes, indicating hard material with high undrained shear strength.

2.3.4. Soil Parameters

See Table 1 for recommended soil parameters for design. See Appendix 6.6 for preliminary calculations.

Table 1: Recommended Soil Parameters (Drained Condition)

Location	Unit Weight γ (lb/ft ³)	Friction Angle Φ (DEG)	Cohesion (ksf)
Boring B-1	125	35	0
Boring B-2	125	0	3.25

1. Friction angle based upon SPT N₁₆₀ Correlation and AASHTO LRFD Table 10.4.6.2.4-1.
2. Cohesion based upon SPT N₆₀ and Consistency Index Correlation Table 3.6 from Section 3.15, Page 97 of Principles of Foundation Engineering, Eighth Edition by Braja M. Das.

2.4. Liquefaction Potential

Based on the soil conditions found at the bridge site, seismically induced settlement should not be significant; therefore, there is a low potential for liquefaction in the event of seismic activity. Additionally, the site has a low probability of having an event that would trigger liquefaction (Magnitude<6.0).

3. RECOMMENDATIONS

3.1. Reuse Existing Foundations

The existing culvert footings consist of gravity type concrete footings of unknown geometry. The latest inspection report categorizes them as being in satisfactory condition. The only real deficiencies noted occur directly over the concrete encased water line where both footings are cracked with minor spalls present near the top of footing. There are no other signs of distress on the existing footings and no signs of scour. The proposed strengthening concept proposes to pour a 12" thick concrete arch over the existing corrugated steel culvert. The proposed arch will be

anchored into the top of the existing footings. The only change to the existing footings in terms of loading will be the result of replacing soil with concrete within the thickness of the arch itself (12") and within the limits of the concrete headwalls. This amounts to an additional 25 pcf (weight of concrete less the weight of the soil, 150-125) within a small portion of the total fill area. As a result, it can be concluded that the culvert strengthening will have a negligible effect on the adequacy of the existing footings. This combined with the satisfactory current condition of the footings suggests they are a good candidate for reuse for the culvert strengthening.

3.2. Shallow Foundations for Southern Wingwall

The stiff soil will provide adequate bearing resistance to support a lightly loaded spread footing type wingwall foundation. Due to the relatively short height of wall required, conventional MSE walls, gabion faced MSE walls, gravity block walls, gabion walls, or concrete cantilever walls are all suitable types of walls for this location. Factored bearing resistance and settlement will vary depending on the wall type chosen and the resulting footing width.

A spread footing foundation shall be designed to the parameters in Table 1 and section 2.3.4 of this report. Embankment slopes may be constructed at 1.5:1 with added modified rock fill.

3.3. Deep Foundations

A deep foundation is not recommended for this site as it does not provide an economic advantage over a shallow foundation.

4. **CONSTRUCTION CONSIDERATIONS**

4.1. Water Table

Groundwater was not measured during the subsurface exploration, but it is assumed to be at the stream elevation which was measured at approximately 1112.2 at the North fascia and 1110.8 at the South fascia in May of 2024. Fluctuations with this elevation are expected with the seasonal flows of the stream. Work below this elevation or water elevations of the stream will require dewatering during construction in order to maintain construction in the dry. Discharge of pumped water should be performed in accordance with all federal, state and local regulations which may require a discharge permit.

4.2. Excavation

As required by OSHA regulations, lateral support is required for any excavation depth greater than four feet and where 1.5:1 slope cannot be maintained. Items for temporary earth support should be included in the contract documents. The design of any temporary support of earth (SOE) is the responsibility of the Contractor and should be designed in accordance with MassDOT and AASHTO requirements.

The proposed wingwall construction may require a water barrier system to maintain work in the dry and minimize impacts to the adjacent stream channel and/or wetlands. The water barrier system may consist of sheet pile, sandbags, or a porta dam. The top of the water barrier will need to be set above the 2-year high water elevation.

4.3. Temporary Bridge Foundation

The proposed staging concept consists of utilizing a temporary bridge in order to maintain a single 11' lane of alternating traffic at all times during construction. The temporary bridge should be founded on abutment structures and shall have a maximum allowable bearing pressure of 4 ksf.

4.4. Obstructions

As is typical, there is the potential to encounter obstructions during excavation activities. The proposed wingwalls are to be located adjacent to the existing footing and run out parallel with the roadway. The exact geometry of the existing footings is unknown.

4.5. Protection of Adjacent Structures and Utilities

There is an 8" water main encased in concrete that runs underground along West Mountain Road. There is an access vault located underneath the roadway at the Northwest corner of the bridge approach. There are also overhead electrical lines that run along West Mountain Road on the North Side. All utilities shall be protected during construction. Coordination with the utility companies shall be performed to determine required construction clearances and to determine if any temporary measures to the utilities would be needed.

4.6. Foundation Preparation

The foundation shall be prepared, and a leveling pad shall be provided per the chosen walls manufacturer's recommendations.

4.7. Sequence of Construction Activities

Construction shall be sequenced in order to maintain a single 11'-0" lane of alternating traffic at all times. This can be accommodated by the use of a temporary bridge that spans over the limits of the excavation.

5. **CONCLUSION**

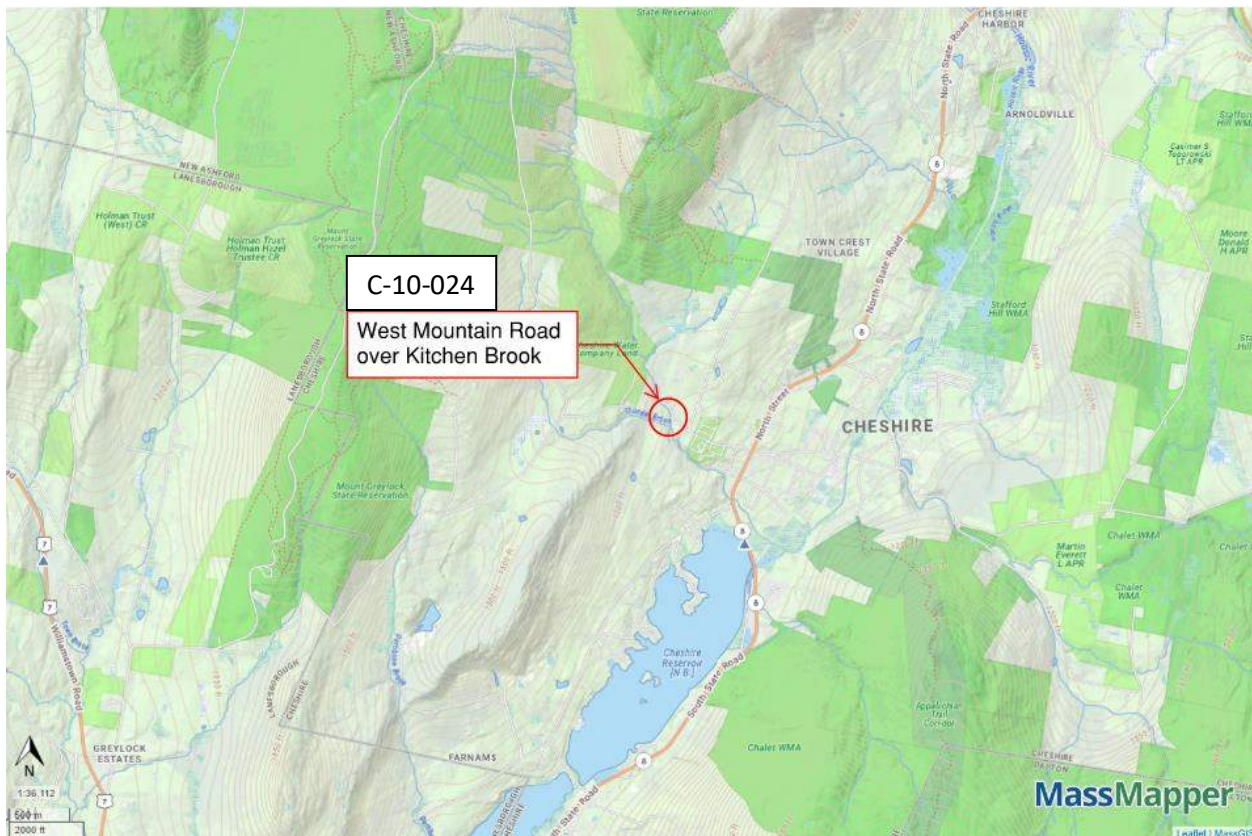
The project site consists of relatively dense material with adequate bearing resistances to support a shallow foundation type wingwall system. Due to the short height of wall required, gravity type

gabion/block walls or conventional/gabion faced MSE walls are all suitable and cost effective options.

APPENDIX

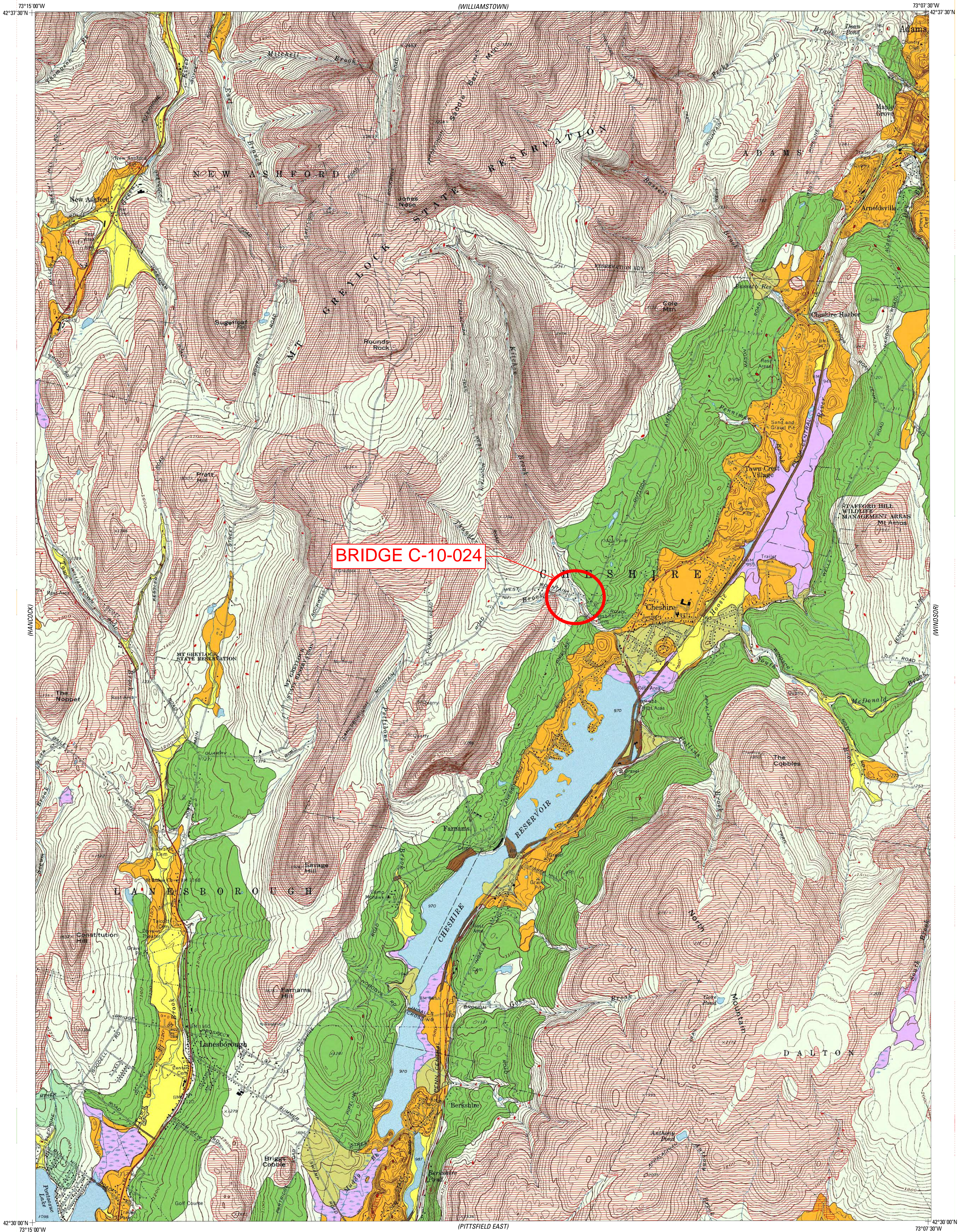
6.1. Project Locus Map

Geotechnical Report: West Mountain Road over Kitchen Brook, C-10-024: Cheshire, MA



APPENDIX

6.2. Geologic Maps



Base from U.S. Geological Survey, 1973
Map was scanned, processed, georeferenced,
rectified, and cropped by the Massachusetts
Geological Survey
Lambert Conformal Conic projection, North American
Datum of 1983
Massachusetts state plane coordinate system,
mainland zone

APPROXIMATE MEAN
DECLINATION, 2018

SCALE 1:24,000
1 0.5 1 MILE
1000 0 1000 2000 3000 4000 5000 6000 7000 FEET
1 0.5 1 KILOMETER
CONTOUR INTERVAL 20 FEET
NATIONAL GEODETIC VERTICAL DATUM OF 1929

MAP LOCATION

Map units were modified from Holmes (1968a) and from
Warren, C.R., 1982, unpublished field map. Some
bedrock outcrops are from Ratcliffe and others (1993)
and Herz (1958). Shallow-bedrock areas were
interpreted from analysis of topographic (lilid) and
soils data. Some units were mapped or revised from
recent field studies and from analysis of 2005
orthophoto images.

Surficial Materials Map of the Cheshire Quadrangle, Massachusetts

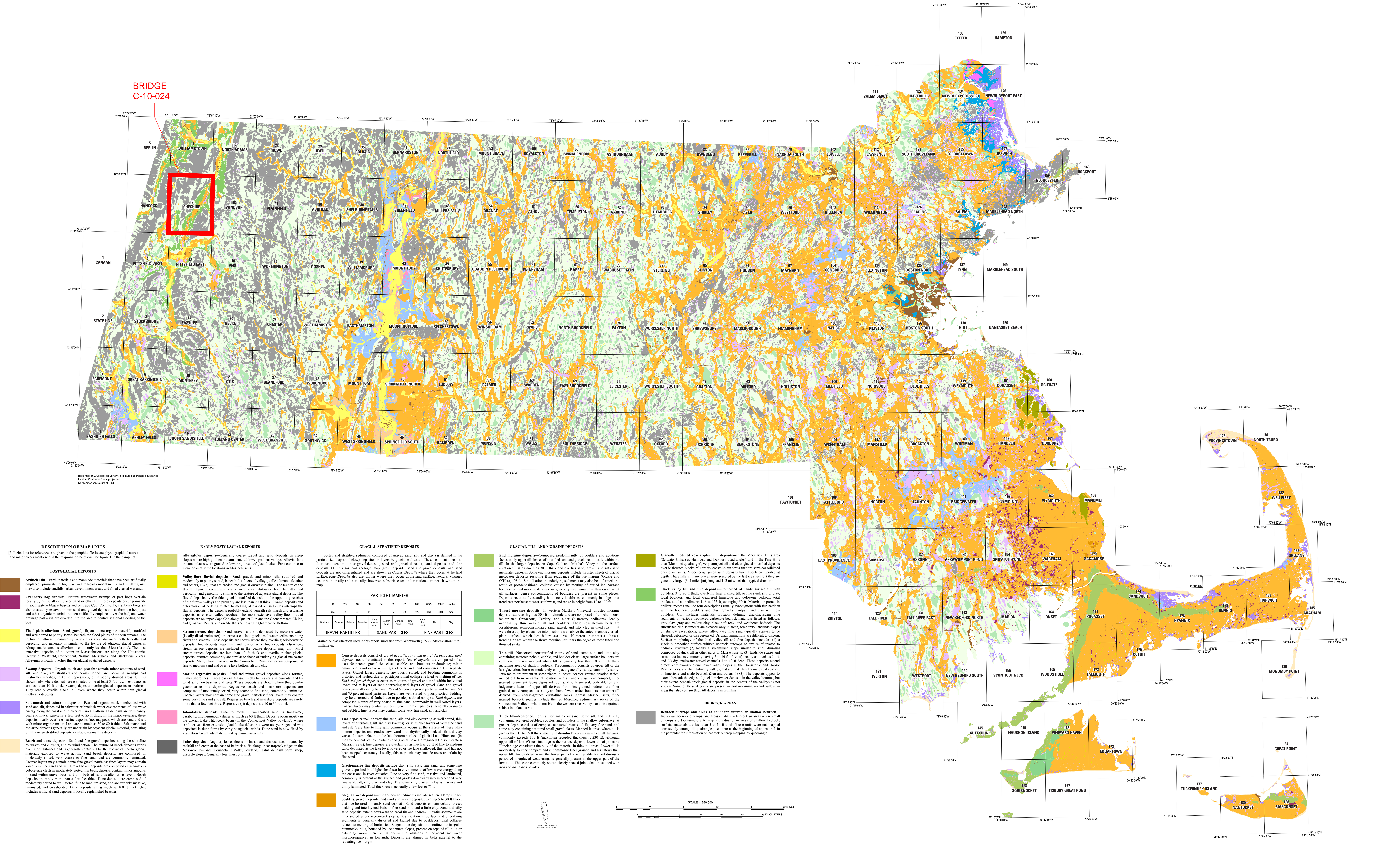
Compiled by
Byron D. Stone and Mary L. DiGiacomo-Cohen
2018

Any use of trade, firm, or product names is for descriptive purposes only and
does not imply endorsement by the U.S. Government

For sale by U.S. Geological Survey, Box 25286, Denver Federal Center,
Denver, CO 80225; <https://store.usgs.gov>; 1-888-ASK-USGS (1-888-275-8747)

Suggested citation: Stone, B.D., and DiGiacomo-Cohen, M.L., comps., 2018,
Surficial materials map of the Cheshire quadrangle, Massachusetts,
quadrangle 12 in Stone, J.R., Stone, B.D., DiGiacomo-Cohen, M.L., and
Maher, S.B., comps., Surficial materials of Massachusetts—A 1:24,000-scale
geologic map database: U.S. Geological Survey Scientific Investigations
Map 3402, 1 sheet, scale 1:24,000, <https://doi.org/10.3133/sim3402>

ISSN 2229-132X (online)
<https://doi.org/10.3133/sim3402>



Index Map of 7.5-Minute Quadrangles in Massachusetts Showing Distribution of Surficial Materials

Surficial Materials of Massachusetts—A 1:24,000-Scale Geologic Map Database

Compiled by
Janet Radway Stone,¹ Byron D. Stone,¹ Mary L. DiGiacomo-Cohen,¹ and Stephen B. Mabey²

¹U.S. Geological Survey, Massachusetts Geological Survey

2018

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For sale by U.S. Geological Survey, Box 3088, Denver Federal Center, Denver, CO 80266. Paper version: \$149.45; \$155.10 (USPS 0-500).

Suggested Citation: Stone, J.R., Stone, B.D., DiGiacomo-Cohen, M.L., and Mabey, S.B., 2018, Index map of 7.5-minute quadrangles in Massachusetts showing distribution of surficial materials, in Stone, J.R., Stone, B.D., DiGiacomo-Cohen, M.L., and Mabey, S.B., eds., Surficial Materials of Massachusetts—A 1:24,000-Scale Geologic Map Database, U.S. Geological Survey Scientific Investigations Map 3402, 1 sheet, 1:24,000 scale.

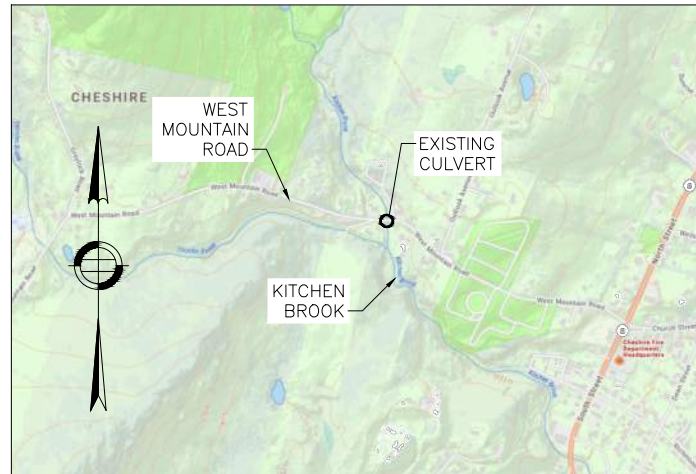
Surficial Materials of Massachusetts—A 1:24,000-Scale Geologic Map Database, U.S. Geological Survey Scientific Investigations Map 3402, 1 sheet, 1:24,000 scale.

https://doi.org/10.3133/sim3402

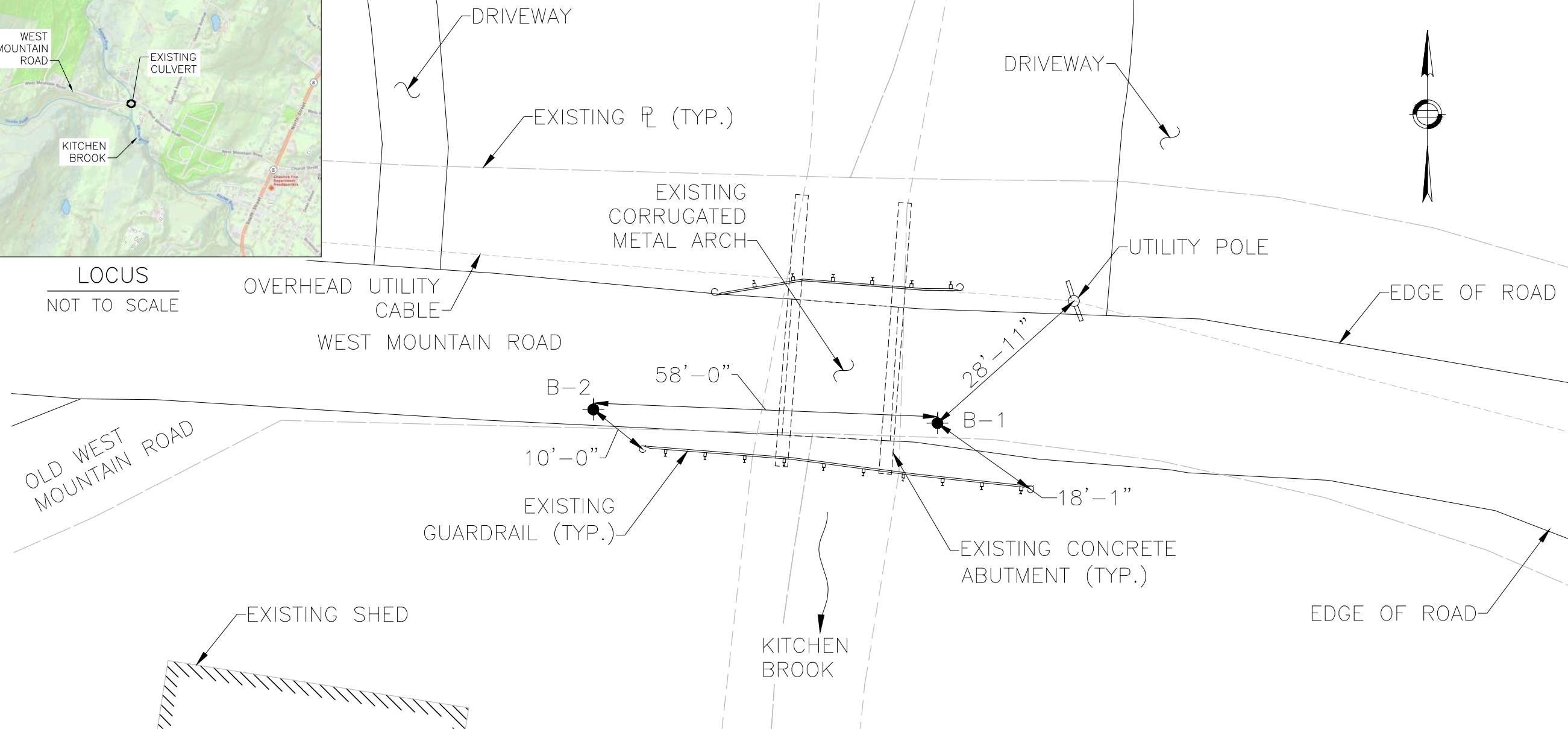
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APPENDIX

6.3. As-Drilled Boring Plan



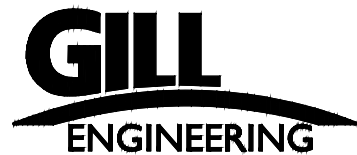
LOCUS
NOT TO SCALE



BORING PLAN
NOT TO SCALE

NOTES:

1. LOCATION OF DRIVE SAMPLE BORINGS ARE SHOWN THUS: ●
2. BORING DEPTHS SHALL BE APPROXIMATELY 50 FEET.
3. BORING LOGS SHALL BE PREPARED AND SUBMITTED TO GILL ENGINEERING ASSOCIATES.
4. BORING LOCATIONS MAY BE ADJUSTED TO AVOID CONFLICTS WITH EXISTING UTILITIES.
5. SOIL SAMPLES SHALL BE PROVIDED TO THE ENGINEER ON-SITE FOR STORAGE AT GILL ENGINEERING.
6. THE BORING CONTRACTOR SHALL BE PREPARED TO OBTAIN ROCK CORES SHOULD ROCK BE ENCOUNTERED AT SHALLOW DEPTHS.



BORING PLAN
TOWN OF CHESHIRE

BORING PLAN FOR CHESHIRE C10024
CULVERT OVER KITCHEN BROOK


Gill Engineering Associates, Inc. 63 Kendrick Street Needham, MA 02494 781-355-7100 www.gill-eng.com


PLAN VIEW
6/29/2023

SHEET
01
OF 01

APPENDIX

6.4. Boring Logs

		Gill Engineering Associates, Inc. 63 Kendrick Street Needham, MA 02494				Boring No. B-1	
		Page 1 of 1					
City/Town: Cheshire		Bridge Number: C-10-024		Project File Number:		Contract Number:	
Location: South Approach				Date & Time Started: 9/25/23 at 10:15am			Total Hours: 4.0
Groundwater Depth (Feet): 15		Date & Time: N/A		Date & Time Completed: 9/25/23 at 2:20pm			
Coordinates: N 61 ° 09' 10" E 71 ° 24' 24"				Driller's Company & Name: Richard Posa NEBC			
Ground Elevation (Feet): 1124+/-				Gill Representative: Kyle Coleman			
Depth (Feet)	Sample Number	Depth Range (Feet)	Blow Counts per 6 Inches	Recovery (inches)	Field Description	Strata Changes	
			Coring Times Minutes per Foot				
-	S1	0-2	9-15-14-19	16	Dry, medium dense, light brown-grey FINE SAND with some coarse sand	3.0	
5	S2	5-7	15-8-4-12	8	Moist, loose, light grey SAND with some fine gravel	13.0	
10	S3	10-12	10-9-6-4	9	Moist, medium dense, grey SAND and fine and coarse GRAVEL		
15	S4	15-17	41-36-50/3"	5	Wet, dense to very dense, grey SAND and GRAVEL with traces of clay		
20	S5	20-22	24-32-38-37	15	Wet, silty, grey CLAY with some fine cobbles and coarse gravel	25.0	
25	S6	25-27	50/0" REFUSAL	0	No Recovery		
30		28	ROCK CORE TAKEN				
Remarks:				Arrow-Board: Signs: Cones:		Protective Device – Stand: Box: Well Depth: Solid Pipe: Stick Up Pipe: Screen Pipe:	
Penetration Resistance (N) Guide						Type of Drill Rig: B53	
Cohesionless Soils (Sands, Gravels)			Cohesive Soils (Silts, Clays)			Casing Type: FJ Size: 4" Hammer Weight: 140lbs Fall: 30" Depth:	
Relative Density	Penetration Resistance		Consistency	Penetration Resistance		Sampler Type: SS Size: 1-3/8" Automatic Hammer Weight: 140lbs Safety Hammer Weight: Donut Hammer Weight: Fall: 30"	
Very Loose	0 – 4		Very Soft	0 – 2			
Loose	4 – 10		Soft	2 – 4			
Medium Dense	10 – 30		Medium Stiff	4 – 8			
Dense	30 – 50		Stiff	8 – 15			
Very Dense	Over 50		Very Stiff	15 – 30			
			Hard	Over 30			
N = Sum of Second and Third 6" Blow counts						Core Barrel Type: NQ Size: 1-7/8"	
Terms Used for Second Entry of Descriptions: and = 40-50%, some = 10-40%, trace = 10% or less							

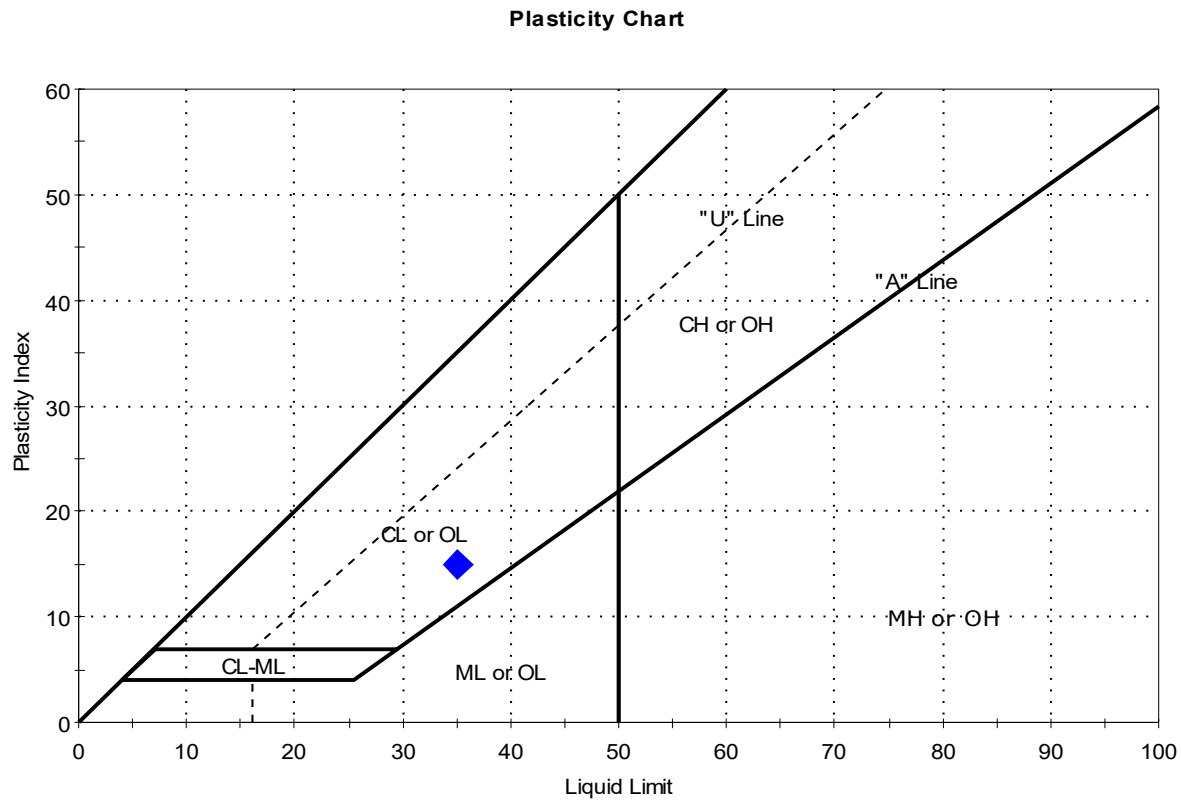
		Gill Engineering Associates, Inc. 63 Kendrick Street Needham, MA 02494			Boring No. B-2	
					Page 1 of 1	
City/Town: Cheshire		Bridge Number: C-10-024		Project File Number:		Contract Number:
Location: South Approach				Date & Time Started: 9/25/23 at 3:15pm		Total Hours: 4.5
Groundwater Depth (Feet): 15		Date & Time: N/A		Date & Time Completed: 9/26/23 at 2:30pm		
Coordinates: N 61° 09' 10" E 71° 24' 27"				Driller's Company & Name: Richard Posa NEBC		
Ground Elevation (Feet): 1123.2				Gill Representative: Kyle Coleman		
Depth (Feet)	Sample Number	Depth Range (Feet)	Blow Counts per 6 Inches	Recovery (inches)	Field Description	Strata Changes
			Coring Times Minutes per Foot			
-	S1	0-2	10-10-9-11	11	Dry, loose to medium dense, brown SAND	13.0
-						
-						
-						
5	S2	5-7	10-7-7-10	1	Moist, loose, dark grey SAND	
-						
-						
-						
10	S3	10-12	28-17-11-4	11	Moist, medium dense, dark grey SAND with Some fine cobbles	
-						
-						
15	S4	15-17	9-14-17-19	7	Wet, medium dense, brown-tan SAND and stiff CLAY with traces of coarse sand	
-						
-						
-						
20	S5	20-22	11-18-20-27	19	Wet, very stiff, brown-tan clay and medium dense fine SAND	
-						
-						
-						
25	S6	25-27	13-16-26-26	7	Wet, very stiff, brown-tan with layers of light grey CLAY with traces of medium dense sand	
-						
-						
-						
-						
30		30	ROCK CORE TAKEN			
Remarks:				Arrow-Board: Signs: Cones:		Protective Device – Stand: Box: Well Depth: Solid Pipe: Stick Up Pipe: Screen Pipe:
Penetration Resistance (N) Guide						Type of Drill Rig: B53
Cohesionless Soils (Sands, Gravels)			Cohesive Soils (Silts, Clays)			Casing Type: FJ Size: 4"
Relative Density	Penetration Resistance	Consistency	Penetration Resistance	Hammer Weight: 140lbs		
Very Loose	0 – 4	Very Soft	0 – 2	Fall: 30"		
Loose	4 – 10	Soft	2 – 4	Depth:		
Medium Dense	10 – 30	Medium Stiff	4 – 8	Sampler Type: SS Size: 1-3/8"		
Dense	30 – 50	Stiff	8 – 15	Automatic Hammer Weight: 140lbs		
Very Dense	Over 50	Very Stiff	15 – 30	Safety Hammer Weight:		
		Hard	Over 30	Donut Hammer Weight:		
N = Sum of Second and Third 6" Blow counts						Fall: 30"
Terms Used for Second Entry of Descriptions: and = 40-50%, some = 10-40%, trace = 10% or less				Core Barrel Type: NQ Size: 1-7/8"		

APPENDIX

6.5. Clay Sample Testing Results

Client:	Gill Engineering Associates, Inc.		
Project:	C10024		
Location:	Cheshire, MA	Project No:	GTX-318007
Boring ID:	B-2	Sample Type:	tube
Sample ID:	S4-5	Test Date:	10/25/23
Depth :	15-22'	Test Id:	740200
Test Comment:	---		
Visual Description:	Moist, reddish brown clay		
Sample Comment:	---		

Atterberg Limits - ASTM D4318



Symbol	Sample ID	Boring	Depth	Natural Moisture Content, %	Liquid Limit	Plastic Limit	Plasticity Index	Liquidity Index	Soil Classification
◆	S4-5	B-2	15-22'	15	35	20	15	-0.3	

Sample Prepared using the WET method

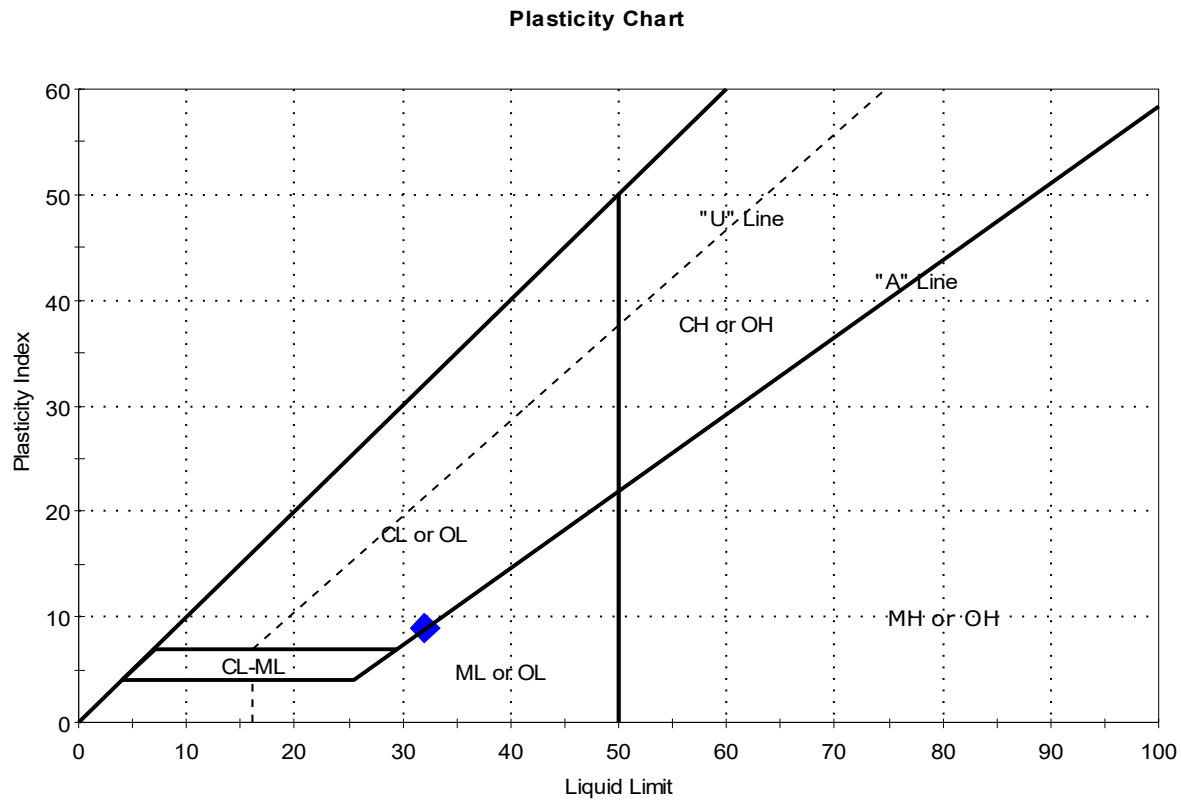
Dry Strength: HIGH

Dilatancy: SLOW

Toughness: LOW

Client:	Gill Engineering Associates, Inc.		
Project:	C10024		
Location:	Cheshire, MA	Project No:	GTX-318007
Boring ID:	B-2	Sample Type:	tube
Sample ID:	S5	Test Date:	10/25/23
Depth :	20-22'	Test Id:	740201
Test Comment:	---		
Visual Description:	Moist, brown clay		
Sample Comment:	---		

Atterberg Limits - ASTM D4318



Symbol	Sample ID	Boring	Depth	Natural Moisture Content, %	Liquid Limit	Plastic Limit	Plasticity Index	Liquidity Index	Soil Classification
◆	S5	B-2	20-22'	20	32	23	9	-0.3	

Sample Prepared using the WET method

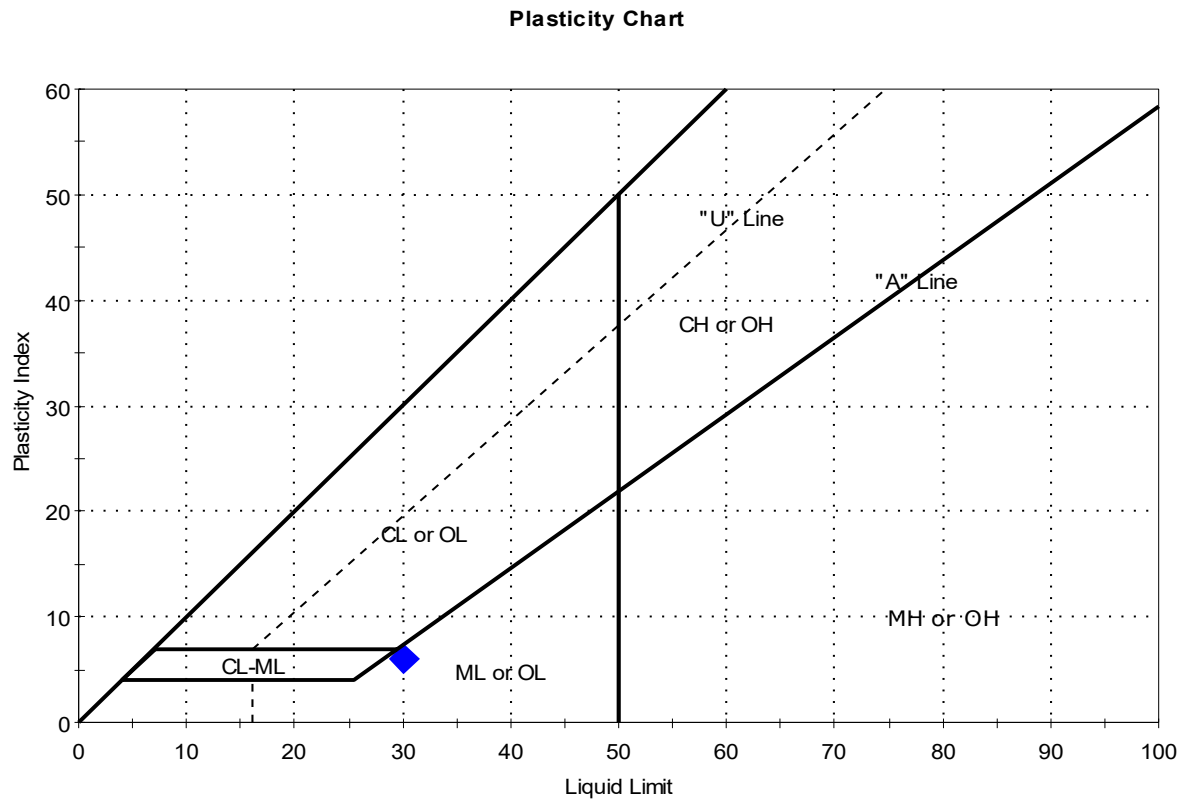
Dry Strength: HIGH

Dilatancy: SLOW

Toughness: LOW

Client:	Gill Engineering Associates, Inc.		
Project:	C10024		
Location:	Cheshire, MA	Project No:	GTX-318007
Boring ID:	B-2	Sample Type:	tube
Sample ID:	S6	Test Date:	10/26/23
Depth :	25-27'	Test Id:	740202
Test Comment:	---		
Visual Description:	Moist, brown silt		
Sample Comment:	---		

Atterberg Limits - ASTM D4318



Symbol	Sample ID	Boring	Depth	Natural Moisture Content, %	Liquid Limit	Plastic Limit	Plasticity Index	Liquidity Index	Soil Classification
◆	S6	B-2	25-27'	21	30	24	6	-0.5	

Sample Prepared using the WET method

Dry Strength: VERY HIGH

Dilatancy: SLOW

Toughness: LOW

APPENDIX

6.6. Preliminary Design Calculations

Geotechnical Calculations - Boring B-1

C-10-024

References:

1. AASHTO LRFD Bridge Design Specifications, 9th Edition, 2020
2. MassDOT LRFD Bridge Manual, 2024

Calc Narrative:

For boring B-1, the majority of the soil was classified as sand and therefore the soil at B-1 will be treated as granular soil.

Soil Strength: (Ref 1 - 10.4.6.2)

Drained strength of granular soils, Ref 1 - 10.4.6.2.4

If SPT N values are used, they shall be corrected for the effects of overburden pressure determined as:

$$N_1 = C_N N \quad (\text{Ref 1 - Eq. 10.4.6.2.4-1})$$

Where
$$C_N = \left[0.77 \log_{10} \left(\frac{40}{\sigma'_v} \right) \right] < 2.0$$

σ'_v = vertical effective stress (ksf)

N = uncorrected SPT blow count (blows/ft)

SPT values should also be corrected for hammer efficiency, determined as:

$$N_{60} = (ER/60\%)N \quad (\text{Ref 1 - Eq. 10.4.6.2.4-2})$$

Where

ER = hammer efficiency expressed as percent of theoretical free fall energy delivered by the hammer system actually used.

Therefore, when SPT blow counts have been corrected for both overburden effects and hammer efficiency effects, the resulting corrected blow count shall be denoted as N_{160} , determined as:

$$N_{160} = C_N N_{60} \quad (\text{Ref 1 - Eq. 10.4.6.2.4-3})$$

The soil friction angle can then be determined based on the following table:

Ref 1 - Table 10.4.6.2.4-1		
N_{160}	ϕ_f (low)	ϕ_f (high)
<4	25	30
4	27	32
10	30	35
30	35	40
50	38	43

Geotechnical Calculations - Boring B-1

C-10-024

Determine friction angle based on soil profile of closest boring:

Boring # = B-1
 Soil Unit Weight = 0.125 kcf
 Water Unit Weight = 0.0624 kcf

Water Table Depth = 15.00 ft
 Ground Elevation = 1123.00 ft

Layer #	Depth to Bottom of Layer	Midpoint of Sample	h_1	h_2	Layer Description
1	4.00 ft	2.00 ft	2.00 ft	0.00 ft	Medium Dense Fine Sand
2	13.00 ft	8.50 ft	8.50 ft	0.00 ft	Loose-Medium Dense Sand
3	18.00 ft	15.50 ft	15.00 ft	0.50 ft	Dense-Very Dense Sand and Gravel
4	25.00 ft	21.50 ft	15.00 ft	6.50 ft	Hard Silty Clay
5	38.00 ft	33.00 ft	15.00 ft	18.00 ft	Bedrock

Layer #	σ'_v	C_N	N	Hammer Efficiency	N_{60}	N_{160}
1	0.250 ksf	1.70	29	0.80	39	66
2	1.063 ksf	1.21	13.5	0.80	18	22
3	1.906 ksf	1.02	77	0.80	103	104
4	2.282 ksf	0.96	70	0.80	93	89
5	3.002 ksf	0.87	n/a	0.80	-	-

Layer #	ϕ_f (low)	ϕ_f (high)	ϕ_f (avg)	Start El.	End El.
1	38	43	40	1123.00 ft	1119.00 ft
2	33	38	35	1119.00 ft	1110.00 ft
3	38	43	40	1110.00 ft	1105.00 ft
4	38	43	40	1105.00 ft	1098.00 ft
5	-	-	-	1098.00 ft	1085.00 ft

Geotechnical Calculations - Southeast Wingwall Bearing ResistanceC-10-024**References:**

1. AASHTO LRFD Bridge Design Specifications, 9th Edition, 2020
2. MassDOT LRFD Bridge Manual, 2024

The proposed wingwall at the southeast corner of the bridge will be founded on the existing soil defined in boring B-1. The following calculations provide the bearing resistance of the soil that the wingwall will be founded on.

Note that the proposed bottom of wall elevation for the wingwalls is 110.9 ft +/- (14.5 ft below grade). The minimum soil friction angle calculated for boring B-1 was found to be 35, which represents dense material.

Bearing Resistance of Soil: (Ref 1 - 10.6.3.1)

Factored Resistance, $q_R = \phi_b q_n$ (Ref 1 - Eq. 10.6.3.1.1-1)

$$\phi_b = 0.45 \quad (\text{Ref 1 - Table 10.5.5.2.2-1})$$

The nominal bearing resistance of a soil layer, in ksf, should be taken as:

$$q_n = cN_{cm} + \gamma D_f N_{qm} C_{wq} + 0.5 \gamma B N_{\gamma m} C_{w\gamma} \quad (\text{Ref 1 - Eq. 10.6.3.1.2a-1})$$

Where: $N_{cm} = N_c s_c i_c$ (Ref 1 - Eq. 10.6.3.1.2a-2)

$$N_{qm} = N_q s_q d_q i_q \quad (\text{Ref 1 - Eq. 10.6.3.1.2a-3})$$

$$N_{\gamma m} = N_\gamma s_\gamma i_\gamma \quad (\text{Ref 1 - Eq. 10.6.3.1.2a-4})$$

$$\text{Unit Wt.} = 0.125 \text{ kcf}$$

$$c = 0.00 \text{ ksf} \quad (\text{cohesion, taken as undrained shear strength, 0 for granular soil})$$

$$\phi_f = 36 \text{ deg} \quad (\text{minimum value for Boring B-1})$$

$$N_c = 50.6 \quad (\text{Ref 1 - Table 10.6.3.1.2a-1})$$

$$N_q = 37.8 \quad (\text{Ref 1 - Table 10.6.3.1.2a-1})$$

$$N_\gamma = 56.3 \quad (\text{Ref 1 - Table 10.6.3.1.2a-1})$$

$$D_f = 2 \text{ ft} \quad (\text{minimum allowable embedment})$$

$$B = 11.0 \text{ ft} \quad (\text{nominal footing width})$$

Per Ref 1 - 10.6.3.1, where loads are eccentric, the effective footing dimensions, L' and B' , as specified in Article 10.6.1.3, shall be used instead of the overall dimensions L and B in all equations, tables, and figures pertaining to bearing resistance.

$$B' = B - 2e_B \quad (\text{Ref 1 - Eq. 10.6.1.3-1})$$

$$L' = L - 2e_L \quad (\text{Ref 1 - Eq. 10.6.1.3-1})$$

Eccentricity in L direction can typically be neglected in abutment design, therefore $L' = L$

$$e_B = 3.67 \text{ ft} \quad (1/3 B, \text{ maximum } e \text{ allowed by code, Ref 1 - 10.6.3.3})$$

$$B' = 3.67 \text{ ft}$$

$$L = 22.00 \text{ ft} \quad (\text{approximate length of footing})$$

Geotechnical Calculations - Southeast Wingwall Bearing Resistance

C-10-024

$$\begin{aligned}
 C_{wq} &= 0.75 && (\text{Ref 1 - Table 10.6.3.1.2a-2}) \\
 C_{wy} &= 0.5 && (\text{Ref 1 - Table 10.6.3.1.2a-2}) \\
 s_c &= 1.12 && (\text{Ref 1 - Table 10.6.3.1.2a-3}) \\
 s_y &= 0.80 && (\text{Ref 1 - Table 10.6.3.1.2a-3}) \\
 s_q &= 1.36 && (\text{Ref 1 - Table 10.6.3.1.2a-3}) \\
 d_q &= 1.00 && (\text{Ref 1 - 10.6.3.1.2a}) \\
 i_c &= 1.00 && (\text{Ref 1 - C10.6.3.1.2a, for footings with modest embedment, typically ignored}) \\
 i_q &= 1.00 && (\text{Ref 1 - C10.6.3.1.2a, for footings with modest embedment, typically ignored}) \\
 i_y &= 1.00 && (\text{Ref 1 - C10.6.3.1.2a, for footings with modest embedment, typically ignored}) \\
 \\
 N_{cm} &= 56.90 = 50.60 \times 1.12 \times 1.00 \\
 N_{qm} &= 51.53 = 37.80 \times 1.36 \times 1.00 \times 1.00 \\
 N_{ym} &= 45.04 = 56.30 \times 0.80 \times 1.00 \\
 \\
 cN_{cm} &= 0.00 = 0.00 \text{ ksf} \times 56.90 \\
 \gamma D_f N_{qm} C_{wq} &= 9.66 = 0.125 \text{ kcf} \times 2 \text{ ft} \times 51.5 \times 0.75 \\
 0.5 \gamma B N_{ym} C_{wy} &= 5.16 = 0.50 \times 0.125 \text{ kcf} \times 3.67 \text{ ft} \times 45.04 \times 0.5 \\
 \\
 q_n &= 0.00 + 9.66 + 5.16 = 14.82 \text{ ksf} \\
 \\
 q_u &= 0.45 \times 14.82 \text{ ksf} = 6.7 \text{ ksf}
 \end{aligned}$$

Geotechnical Calculations - Southeast Wingwall Bearing Resistance

C-10-024

Settlement Analyses: (Ref I - 10.6.2.4)

Total settlement, including elastic, consolidation, and secondary components may be taken as:

$$S_t = S_e + S_c + S_s \quad (\text{Ref I - Eq. 10.6.2.4.1-1})$$

For cohesionless soils, only elastic settlement is typically considered, therefore $S_t = S_e$

Elastic settlement can be approximated using either the elastic half-space method or the empirical Hough method. Both methods are calculated here for reference.

Elastic Half-Space Method:

$$S_e = \frac{[q_o(1 - \nu^2)\sqrt{A'}]}{144E_s\beta_z} \quad (\text{Ref I - Eq. 10.6.2.4.2-1})$$

Where:

q_o = applied vertical stress (ksf)

A' = effective area of footing (ft^2)

E_s = Young's modulus of soil taken from Article 10.4.6.3

β_z = shape factor taken as specified in table 10.6.2.4.2-1

ν = Poisson's Ratio, taken as specified in Article 10.4.6.3

$$P = 37 \text{ kips} \quad (\text{total vertical load on wingwall, conservatively use Strength I})$$

$$A' = B'L' = 81 \text{ ft}^2 = 3.67 \text{ ft} \times 22.00 \text{ ft}$$

$$q_o = P/A' = 0.5 \text{ ksf} = 37 \text{ kips} / 81 \text{ ft}^2$$

$$E_s = 2.00 \text{ ksi} \quad (\text{Ref I - Table C10.4.6.3-1, loose-medium dense sand})$$

$$\nu = 0.25$$

$$L/B = 6.00 = 22.00 \text{ ft} / 3.67 \text{ ft}$$

$$\text{Footing Type} = \text{Flexible} \quad (\text{Typical spread footing})$$

$$\beta_z = 1.258$$

$$S_e = 0.01 \text{ ft} = \frac{0.5 \text{ ksf} (1 - 0.06) \times 8.98 \text{ ft}}{(144 \times 2.00 \times 1.258)}$$

$$S_e = 0.13 \text{ in}$$

Geotechnical Calculations - Southeast Wingwall Bearing Resistance

C-10-024

Empirical Hough Method:

$$S_e = \sum_{i=1}^n \Delta H_i \quad (\text{Ref 1 - Eq. 10.6.2.4.2-2})$$

Where: $\Delta H_i = H_c \frac{1}{C'} \log \left(\frac{\sigma'_o + \Delta \sigma_v}{\sigma'_o} \right)$ (Ref 1 - Eq. 10.6.2.4.2-3)

n = number of soil layers within zone of stress influence of the footing

H_c = initial height of each layer I (ft)

C' = bearing capacity index from Figure 10.6.2.4.2-1

σ'_o = initial vertical effective stress at the midpoint of layer I (ksf)

Δσ_v = increase in vertical stress at the midpoint of layer I (ksf)

Depth of bottom of footing below grade, d = 15 ft

Increase in vertical stress at point directly below footing is equal to the applied vertical stress, q_o (ksf).

Increase in vertical stress at a depth of z below the bottom of footing are assumed equal to applied load P divided by effective area at point of interest calculated assuming a 2:1 distribution slope, therefore A' = (B'+z)(L'+z)

Layer	Depth to Bottom of Layer	H _c	Midpoint Depth Below Footing, z	σ' _v	A'	Δσ _v (P/A')
1	4.00 ft	4.00 ft	0.00 ft	0.250 ksf	81 ft ²	0.5 ksf
2	13.00 ft	9.00 ft	0.00 ft	1.063 ksf	81 ft ²	0.5 ksf
3	18.00 ft	5.00 ft	1.50 ft	1.906 ksf	121 ft ²	0.3 ksf
4	25.00 ft	7.00 ft	6.50 ft	2.282 ksf	290 ft ²	0.1 ksf
5	38.00 ft	13.00 ft	16.50 ft	3.002 ksf	776 ft ²	0.0 ksf

Layer	N _{I60}	*C'	ΔH
1	66	170	-
2	22	70	-
3	104	200	0.00 ft
4	89	200	0.00 ft
5	-	-	-

*In Figure 10.6.2.4.2-1 Clean well graded fine to coarse Sand was assumed

$$\Sigma = 0.00 \text{ ft} = 0.03 \text{ in}$$

Geotechnical Calculations - Southwest Wingwall Bearing ResistanceC-10-024**References:**

1. AASHTO LRFD Bridge Design Specifications, 9th Edition, 2020
2. MassDOT LRFD Bridge Manual, 2024

The proposed wingwall at the southwest corner of the bridge will be founded on the existing soil defined in boring B-2. The following calculations provide the bearing resistance of the soil that the wingwall will be founded on.

Note that the proposed bottom of wall elevation for the wingwalls is 110.9 ft +/- (14.5 ft below grade). The majority of material found below this depth at boring B-2 was identified (and tested) as hard clay. As such, a conservative value was used for the cohesion (undrained shear strength) with a corresponding friction angle of 0 for determining bearing resistance.

Bearing Resistance of Soil: (Ref 1 - 10.6.3.1)

Factored Resistance, $q_R = \phi_b q_n$ (Ref 1 - Eq. 10.6.3.1.1-1)

$$\phi_b = 0.50 \quad (\text{Ref 1 - Table 10.5.5.2.2-1})$$

The nominal bearing resistance of a soil layer, in ksf, should be taken as:

$$q_n = cN_{cm} + \gamma D_f N_{qm} C_{wq} + 0.5 \gamma B N_{\gamma m} C_{w\gamma} \quad (\text{Ref 1 - Eq. 10.6.3.1.2a-1})$$

Where: $N_{cm} = N_c s_c i_c$ (Ref 1 - Eq. 10.6.3.1.2a-2)

$$N_{qm} = N_q s_q d_q i_q \quad (\text{Ref 1 - Eq. 10.6.3.1.2a-3})$$

$$N_{\gamma m} = N_\gamma s_\gamma i_\gamma \quad (\text{Ref 1 - Eq. 10.6.3.1.2a-4})$$

Unit Wt. = 0.125 kcf

To determine the undrained shear strength, a conservative assumption will be necessary based on the SPT blow counts found in the field. From the Text Book "Principles of Foundation Engineering" Eighth Edition, by Braja M. Das, there is a correlation table of SPT blow counts (N₆₀) and estimated consistency of the cohesive soil vs empirical values to be used for the unconfined compressive strength. It should be noted that the undrained shear strength is equal to 1/2 the unconfined compressive strength.

Table 3.6 Approximate Correlation between CI, N_{60} , and q_u

Standard penetration number, N_{60}	Consistency	CI	Unconfined compression strength, q_u	
			(kN/m ²)	(lb/ft ²)
<2	Very soft	<0.5	<25	500
2-8	Soft to medium	0.5-0.75	25-80	500-1700
8-15	Stiff	0.75-1.0	80-150	1700-3100
15-30	Very stiff	1.0-1.5	150-400	3100-8400
>30	Hard	>1.5	>400	8400

$Suc = 6.50$ ksf (SPT counts >32, Hard Clay, CI around 1.33)

$c = 3.25$ ksf (cohesion, taken as undrained shear strength, 0 for granular soil, $Suc/2$ for cohesive soil)

$\phi_f = 0$ deg (from above)

Geotechnical Calculations - Southwest Wingwall Bearing Resistance

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$$\begin{aligned} N_c &= 5.1 && (\text{Ref 1 - Table 10.6.3.1.2a-1}) \\ N_q &= 1.0 && (\text{Ref 1 - Table 10.6.3.1.2a-1}) \\ N_\gamma &= 0.0 && (\text{Ref 1 - Table 10.6.3.1.2a-1}) \\ D_f &= 2 \text{ ft} && (\text{minimum allowable embedment}) \\ B &= 11.0 \text{ ft} && (\text{nominal footing width}) \end{aligned}$$

Per Ref 1 - 10.6.3.1, where loads are eccentric, the effective footing dimensions, L' and B' , as specified in Article 10.6.1.3, shall be used instead of the overall dimensions L and B in all equations, tables, and figures pertaining to bearing resistance.

$$\begin{aligned} B' &= B - 2e_B && (\text{Ref 1 - Eq. 10.6.1.3-1}) \\ L' &= L - 2e_L && (\text{Ref 1 - Eq. 10.6.1.3-1}) \end{aligned}$$

Eccentricity in L direction can typically be neglected in abutment design, therefore $L' = L$

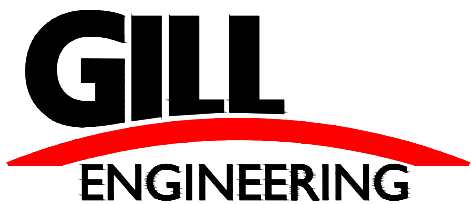
$$\begin{aligned} e_B &= 3.67 \text{ ft} && (1/3 B, \text{ maximum } e \text{ allowed by code, Ref 1 - 10.6.3.3}) \\ B' &= 3.67 \text{ ft} \\ L &= 22.00 \text{ ft} && (\text{approximate length of footing}) \\ C_{wq} &= 0.75 && (\text{Ref 1 - Table 10.6.3.1.2a-2}) \\ C_{w\gamma} &= 0.5 && (\text{Ref 1 - Table 10.6.3.1.2a-2}) \\ s_c &= 1.10 && (\text{Ref 1 - Table 10.6.3.1.2a-3}) \\ s_\gamma &= 1.00 && (\text{Ref 1 - Table 10.6.3.1.2a-3}) \\ s_q &= 1.00 && (\text{Ref 1 - Table 10.6.3.1.2a-3}) \\ d_q &= 1.00 && (\text{Ref 1 - 10.6.3.1.2a}) \\ i_c &= 1.00 && (\text{Ref 1 - C10.6.3.1.2a, for footings with modest embedment, typically ignored}) \\ i_q &= 1.00 && (\text{Ref 1 - C10.6.3.1.2a, for footings with modest embedment, typically ignored}) \\ i_\gamma &= 1.00 && (\text{Ref 1 - C10.6.3.1.2a, for footings with modest embedment, typically ignored}) \end{aligned}$$

$$\begin{aligned} N_{cm} &= 5.65 = 5.14 \times 1.10 \times 1.00 \\ N_{qm} &= 1.00 = 1.00 \times 1.00 \times 1.00 \times 1.00 \\ N_{\gamma m} &= 0.00 = 0.00 \times 1.00 \times 1.00 \end{aligned}$$

$$\begin{aligned} cN_{cm} &= 18.38 = 3.25 \text{ ksf} \times 5.65 \\ \phi D_f N_{qm} C_{wq} &= 0.19 = 0.125 \text{ kcf} \times 2 \text{ ft} \times 1.0 \times 0.75 \\ 0.5 \phi B N_{\gamma m} C_{w\gamma} &= 0.00 = 0.50 \times 0.125 \text{ kcf} \times 3.67 \text{ ft} \times 0.00 \times 0.5 \end{aligned}$$

$$q_n = 18.38 + 0.19 + 0.00 = 18.56 \text{ ksf}$$

$$q_u = 0.50 \times 18.56 \text{ ksf} = 9.3 \text{ ksf}$$



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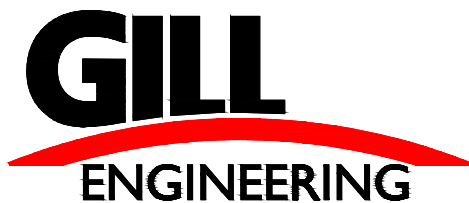
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Geotechnical Calculations - Southwest Wingwall Bearing Resistance

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Settlement Analyses:

Since the clay that is present at the elevation of the proposed bottom of footing and below is hard (blow counts >30) the clay is classified as overconsolidated and therefore settlement is not a concern. This is further confirmed by the fact that this is for a wingwall footing that is lightly loaded.



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MSE Wall Design

C-10-024

References:

1. MassDOT LRFD Bridge Manual 2024
2. AASHTO LRFD Bridge Design Specifications, 9th Edition 2020, with current Interims

Calculation Narrative:

The following calculations determine the overall geometry for the MSE wingwalls along the south side of the roadway and the adequacy for external stability. Final design, including internal stability of the MSE wall system will be submitted by the MSE wall designer chosen by the general contractor.

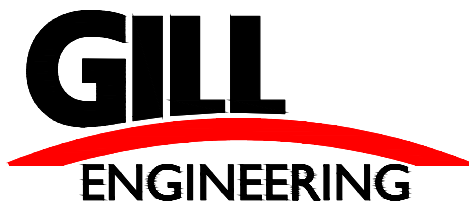
General Input:

Min. Embedment Depth =	2.00 ft
Curb Reveal =	0.50 ft
Safety Curb Chamfer =	0.17 ft

Profile Information:

Grade Break Station 1 =	1015.00 ft
Grade Break Elevation 1 =	1124.25 ft
Grade 1 =	0.64%

Grade Break Station 2 =	1050.00 ft
Grade Break Elevation 2 =	1124.48 ft
Grade 2 =	-0.51%



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MSE Wall Design

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Wall Heights:

Southwest Wall

Wall Length = 20.00 ft

Start Station of SW Wall = 1020.55 ft

End Station of SW Wall = 1040.56 ft

Roadway Cross Slope = 2.00%

Offset = 12.00 ft

Top of Start of SW Wall = 1124.38 ft

Top of End of SW Wall = 1124.51 ft

Use = 1124.50 ft

Grade at Start = 1124.50 ft

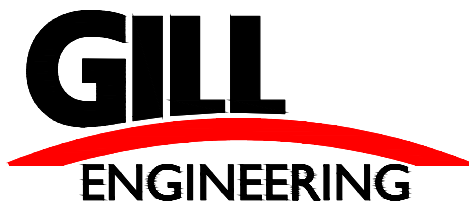
Grade at End = 1111.00 ft

Bottom of Wall at Start = 1120.50 ft

Bottom of Wall at End = 1109.00 ft

Height of Wall at Start = 3.88 ft

Height of Wall at End = 15.51 ft



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MSE Wall Design

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Southeast Wall

Wall Length = 20.00 ft

Start Station of SE Wall = 1059.01 ft

End Station of SE Wall = 1079.00 ft

Roadway Cross Slope = 2.00%

Offset = 12.00 ft

Top of Start of SE Wall = 1124.53 ft

Top of End of SE Wall = 1124.43 ft

Use = 1124.50 ft

Grade at Start = 1111.00 ft

Grade at End = 1124.50 ft

Bottom of Wall at Start = 1109.00 ft

Bottom of Wall at End = 1120.50 ft

Height of Wall at Start = 15.53 ft

Height of Wall at End = 3.93 ft

MSE Wall External Stability - Max Height

C-10-024

References:

1. MassDOT LRFD Bridge Manual 2024
2. AASHTO LRFD Bridge Design Specifications, 9th Edition 2020, with current Interims

Calculation Narrative:

The following calculations determine the overall geometry for the MSE wingwalls along the south side of the roadway and the adequacy for external stability. Final design, including internal stability of the MSE wall system will be submitted by the MSE wall designer chosen by the general contractor.

General Input:

Wall Length, L =	20.00 ft		
Wall Height, H =	15.53 ft		
Base Width, B =	11.00 ft	>	0.70H
Soil Unit Weight =	125 pcf		OK
Retained Soil Friction Angle =	35 deg =	0.61 rad	(minimum value)
Reinforced Soil Friction Angle =	35 deg =	0.61 rad	(gravel borrow)
Foundation Soil Friction Angle =	35 deg =	0.61 rad	(minimum value)
Wall Friction Angle =	23 deg =	0.41 rad	

Applied Loads:

Soil Mass:

Base Width =	11.00 ft		
Wall Height =	15.53 ft		
Soil Mass Area =	171 ft ² =	11.00 ft x	15.53 ft
Soil Mass Weight =	21.35 klf =	171 ft ² x	125 pcf/ 1000

MSE Wall External Stability

C-10-024

Lateral Earth Pressure:

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = 0.27$$

$$\begin{aligned} R &= 4.08 \text{ klf} = 0.50 \times 0.27 \times 0.125 \text{ kcf} \times (15.53 \text{ ft})^2 \\ Y &= 5.18 \text{ ft} = 15.53 \text{ ft} / 3 \\ H &= 3.75 \text{ klf} = 4.08 \text{ klf} \times 0.92 \\ V &= 1.62 \text{ klf} = 4.08 \text{ klf} \times 0.40 \\ X &= -5.50 \text{ ft} \end{aligned}$$

Live Load Surcharge:

The increase in horizontal pressure due to live load surcharge may be estimated as:

$$\Delta_p = k \gamma_s h_{eq} \quad (3.11.6.4-1)$$

where:

$$\begin{aligned} \Delta_p &= \text{constant horizontal earth pressure due to live load surcharge (ksf)} \\ \gamma_s &= \text{total unit weight of soil (kcf)} \\ k &= \text{coefficient of lateral earth pressure} \\ h_{eq} &= \text{equivalent height of soil for vehicular load (ft)} \end{aligned}$$

Table 3.11.6.4-2—Equivalent Height of Soil for Vehicular Loading on Retaining Walls Parallel to Traffic

Retaining Wall Height (ft)	h_{eq} (ft) Distance from wall backface to edge of traffic	
	0.0 ft	1.0 ft or Further
5.0	5.0	2.0
10.0	3.5	2.0
≥20.0	2.0	2.0

Equivalent heights of soil, h_{eq} , for highway loadings on abutments and retaining walls may be taken from Tables 3.11.6.4-1 and 3.11.6.4-2. Linear interpolation shall be used for intermediate wall heights.

The wall height shall be taken as the distance between the surface of the backfill and the bottom of the footing along the pressure surface being considered.

The load factor for both vertical and horizontal components of live load surcharge shall be taken as specified in Table 3.4.1-1 for live load surcharge.

$$h_{eq} = 2.00 \text{ ft}$$

$$\begin{aligned} \Delta &= 1.05 \text{ klf} = 0.27 \times 0.125 \text{ kcf} \times 2.00 \text{ ft} \times 15.53 \text{ ft} \\ Y &= 7.76 \text{ ft} = 15.53 \text{ ft} / 2 \\ H &= 0.97 \text{ klf} = 1.05 \text{ klf} \times 0.92 \\ V &= 0.42 \text{ klf} = 1.05 \text{ klf} \times 0.40 \\ X &= -5.50 \text{ ft} \end{aligned}$$

MSE Wall External Stability

C-10-024

For bearing evaluation, also include vertical component of live load surcharge.

$$P = 2.75 \text{ klf} = 0.125 \text{ kcf} \times 2.00 \text{ ft} \times 11.00 \text{ ft}$$

Vehicular Impact:

$$\begin{aligned} P &= 23.0 \text{ k} \quad (\text{Ref I - Table 3.3.2-1, TL 2}) \\ H &= 2.00 \text{ ft} \quad (\text{Ref I - Table 3.3.2-1, TL 2}) \\ L &= 20.00 \text{ ft} \quad (\text{Ref I - 3.3.2.4, entire wall length can be used to resist impact}) \end{aligned}$$

$$\begin{aligned} P &= 1.15 \text{ klf} = 23.0 \text{ k} / 20.00 \text{ ft} \\ Y &= 17.53 \text{ ft} = 15.53 \text{ ft} + 2.00 \text{ ft} \end{aligned}$$

Load Factors:

	Strength I		Extreme II
	Bearing	Sliding/Ecc.	
EV	1.35	1.00	1.00
EH	1.50	1.50	1.00
LS	1.75	1.75	0.50
CT	0.00	0.00	1.00

Strength I, Bearing Evaluation:

Loads:

	Unfactored	Load Factor	Factored	V or H
EV	21.35 klf	1.35	28.82 klf	V
EHh	3.75 klf	1.50	5.62 klf	H
EHv	1.62 klf	1.50	2.43 klf	V
LSH	0.97 klf	1.75	1.69 klf	H
LSv	0.42 klf	1.75	0.73 klf	V
LS-Vert	2.75 klf	1.75	4.81 klf	V
CT	1.15 klf	0.00	0.00 klf	H

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	H	Y	V	X	M
EV	0.00 klf	-	28.82 klf	0.00 ft	0.00 k-ft
EHh	5.62 klf	5.18 ft	0.00 klf	-	29.11 k-ft
EHv	-	-	2.43 klf	-5.50 ft	-13.34 k-ft
LSH	1.69 klf	7.76 ft	0.00 klf	-	13.12 k-ft
LSv	-	-	0.73 klf	-5.50 ft	-4.01 k-ft
LS-Vert	0.00 klf	-	4.81 klf	-	0.00 k-ft
CT	0.00 klf	17.53 ft	0.00 klf	-	0.00 k-ft
	<u>7.31 klf</u>		<u>36.79 klf</u>		<u>24.88 k-ft</u>

Eccentricity, $e = 0.68 \text{ ft} = 24.88 \text{ k-ft} / 36.79 \text{ klf}$

Effective Width, $B' = 9.65 \text{ ft} = 11.00 \text{ ft} - 2 \times 0.68 \text{ ft}$

Applied Pressure = $3.81 \text{ ksf} = 36.79 \text{ klf} / 9.65 \text{ ft}$

Ultimate Bearing Capacity = 6.67 ksf (see bearing capacity calculations, minimum from B-1/B-2 used)

Applied	<	Allowable
3.81 ksf	<	6.67 ksf

OK

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Strength I, Sliding and Eccentricity Evaluation:

Loads:

	Unfactored	Load Factor	Factored	V or H
EV	21.35 klf	1.00	21.35 klf	V
EHh	3.75 klf	1.50	5.62 klf	H
EHv	1.62 klf	1.50	2.43 klf	V
LSH	0.97 klf	1.75	1.69 klf	H
LSv	0.42 klf	1.75	0.73 klf	V
LS-Vert	2.75 klf	0.00	0.00 klf	V
CT	1.15 klf	0.00	0.00 klf	H

	H	Y	V	X	M
EV	0.00 klf	-	21.35 klf	0.00 ft	0.00 k-ft
EHh	5.62 klf	5.18 ft	0.00 klf	-	29.11 k-ft
EHv	-	-	2.43 klf	-5.50 ft	-13.34 k-ft
LSH	1.69 klf	7.76 ft	0.00 klf	-	13.12 k-ft
LSv	-	-	0.73 klf	-5.50 ft	-4.01 k-ft
LS-Vert	0.00 klf	-	0.00 klf	-	0.00 k-ft
CT	0.00 klf	17.53 ft	0.00 klf	-	0.00 k-ft
	<u>7.31 klf</u>		<u>24.51 klf</u>		<u>24.88 k-ft</u>

Eccentricity Check:

$$\text{Eccentricity, } e = 1.02 \text{ ft} = \frac{24.88 \text{ k-ft}}{24.51 \text{ klf}}$$

Per Ref 1 - 11.6.3.3, for foundations on soil, the location of the resultant of the reaction forces shall be within the middle two-thirds of the base width.

$$\text{Allowable } e = 3.67 \text{ ft} > 1.02 \text{ ft} \quad \text{OK}$$

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Sliding Check:

10.6.3.4—Failure by Sliding

Failure by sliding shall be investigated for footings that support horizontal or inclined load and/or are founded on slopes.

For foundations on clay soils, the possible presence of a shrinkage gap between the soil and the foundation shall be considered. If passive resistance is included as part of the shear resistance required for resisting sliding, consideration shall also be given to possible future removal of the soil in front of the foundation.

The factored resistance against failure by sliding, in kips, shall be taken as:

$$R_g = \phi R_u = \phi_s R_s + \phi_{ep} R_{ep} \quad (10.6.3.4-1)$$

where:

- ϕ = resistance factor (dim)
 R_u = nominal sliding resistance against failure by sliding (kips)
 ϕ_s = resistance factor for shear resistance between soil and foundation specified in Table 10.5.5.2.2-1
 R_s = nominal sliding resistance between soil and foundation (kips)
 ϕ_{ep} = resistance factor for passive resistance specified in Table 10.5.5.2.2-1
 R_{ep} = nominal passive resistance of soil available throughout the design life of the structure (kips)

If the soil beneath the footing is cohesionless, the nominal sliding resistance between soil and foundation shall be taken as:

$$R_s = CV \tan \phi_f \quad (10.6.3.4-2)$$

for which:

- C = 1.0 for concrete cast against soil
= 0.8 for precast concrete footing

where:

- ϕ_f = internal friction angle of drained soil (degrees)
 V = total vertical force (kips)

$$\text{Min. } \phi = 35.00 \text{ deg}$$

$$\tan(\phi) = 0.70$$

$$C = 1$$

$$V = 24.51 \text{ klf}$$

$$R = 17.16 \text{ klf} = 1 \times 24.51 \text{ klf} \times 0.70$$
$$\phi = 0.9 \quad (\text{Ref 1 - Table 10.5.5.2.2-1, soil on soil})$$

$$\phi R_n = 15.44 \text{ klf} = 0.90 \times 17.16 \text{ klf}$$

$$\text{Applied H} = 7.31 \text{ klf} < 15.44 \text{ klf} \quad \text{OK}$$

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Extreme 2 Evaluation:

Loads:

	Unfactored	Load Factor	Factored	V or H
EV	21.35 klf	1.00	21.35 klf	V
EHh	3.75 klf	1.00	3.75 klf	H
EHv	1.62 klf	1.00	1.62 klf	V
LSH	0.97 klf	0.50	0.48 klf	H
LSv	0.42 klf	0.50	0.21 klf	V
LS-Vert	2.75 klf	0.00	0.00 klf	V
CT	1.15 klf	1.00	1.15 klf	H

	H	Y	V	X	M
EV	0.00 klf	-	21.35 klf	0.00 ft	0.00 k-ft
EHh	3.75 klf	5.18 ft	0.00 klf	-	19.41 k-ft
EHv	-	-	1.62 klf	-5.50 ft	-8.90 k-ft
LSH	0.48 klf	7.76 ft	0.00 klf	-	3.75 k-ft
LSv	-	-	0.21 klf	-5.50 ft	-1.15 k-ft
LS-Vert	0.00 klf	-	0.00 klf	-	0.00 k-ft
CT	1.15 klf	17.53 ft	0.00 klf	-	20.16 k-ft
	<u>5.38 klf</u>		<u>23.18 klf</u>		<u>33.27 k-ft</u>

Eccentricity Check:

$$\text{Eccentricity, } e = 1.44 \text{ ft} = \frac{33.27 \text{ k-ft}}{23.18 \text{ klf}}$$

Per Ref 1 - 11.6.5.1, for foundations on soil and rock, the location of the resultant of the reaction forces shall be within the middle eight-tenths of the base width for Extreme Event.

$$\text{Allowable } e = 4.40 \text{ ft} > 1.44 \text{ ft} \quad \text{OK}$$

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Sliding Check:

$$\text{Min. } \phi = 35.00 \text{ deg}$$

$$\tan(\phi) = 0.70$$

$$C = 1$$

$$V = 23.18 \text{ klf}$$

$$R = 16.23 \text{ klf} = 1 \times 23.18 \text{ klf} \times 0.70$$

$$\phi = 1 \text{ (Ref 1 - Extreme Event)}$$

$$\phi R_n = 16.23 \text{ klf} = 1.00 \times 16.23 \text{ klf}$$

$$\text{Applied H} = 5.38 \text{ klf} < 16.23 \text{ klf} \quad \text{OK}$$

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References:

1. MassDOT LRFD Bridge Manual 2024
2. AASHTO LRFD Bridge Design Specifications, 9th Edition 2020, with current Interims

Calculation Narrative:

The following calculations determine the overall geometry for the MSE wingwalls along the south side of the roadway and the adequacy for external stability. Final design, including internal stability of the MSE wall system will be submitted by the MSE wall designer chosen by the general contractor.

General Input:

Wall Length, L =	20.00 ft		
Wall Height, H =	4.00 ft		
Base Width, B =	6.00 ft	>	0.70H
Soil Unit Weight =	125 pcf		OK
Retained Soil Friction Angle =	35 deg =	0.61 rad	(minimum value)
Reinforced Soil Friction Angle =	35 deg =	0.61 rad	(gravel borrow)
Foundation Soil Friction Angle =	35 deg =	0.61 rad	(minimum value)
Wall Friction Angle =	23 deg =	0.41 rad	(2/3 * ϕ)

Applied Loads:

Soil Mass:

Total Width =	6.00 ft		
Wall Height =	4.00 ft		
Soil Mass Area =	24 ft ² =	6.00 ft x	4.00 ft
Soil Mass Weight =	3.00 klf =	24 ft ² x	125 pcf/ 1000

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Lateral Earth Pressure:

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = 0.27$$

$$\begin{aligned} R &= 0.27 \text{ klf} = 0.50 \times 0.27 \times 0.125 \text{ kcf} \times (4.00 \text{ ft})^2 \\ Y &= 1.33 \text{ ft} = 4.00 \text{ ft} / 3 \\ H &= 0.25 \text{ klf} = 0.27 \text{ klf} \times 0.92 \\ V &= 0.11 \text{ klf} = 0.27 \text{ klf} \times 0.40 \\ X &= -3.00 \text{ ft} \end{aligned}$$

Live Load Surcharge:

The increase in horizontal pressure due to live load surcharge may be estimated as:

$$\Delta_p = k \gamma_s h_{eq} \quad (3.11.6.4-1)$$

where:

$$\begin{aligned} \Delta_p &= \text{constant horizontal earth pressure due to live load surcharge (ksf)} \\ \gamma_s &= \text{total unit weight of soil (kcf)} \\ k &= \text{coefficient of lateral earth pressure} \\ h_{eq} &= \text{equivalent height of soil for vehicular load (ft)} \end{aligned}$$

Table 3.11.6.4-2—Equivalent Height of Soil for Vehicular Loading on Retaining Walls Parallel to Traffic

Retaining Wall Height (ft)	h_{eq} (ft) Distance from wall backface to edge of traffic	
	0.0 ft	1.0 ft or Further
5.0	5.0	2.0
10.0	3.5	2.0
≥20.0	2.0	2.0

Equivalent heights of soil, h_{eq} , for highway loadings on abutments and retaining walls may be taken from Tables 3.11.6.4-1 and 3.11.6.4-2. Linear interpolation shall be used for intermediate wall heights.

The wall height shall be taken as the distance between the surface of the backfill and the bottom of the footing along the pressure surface being considered.

The load factor for both vertical and horizontal components of live load surcharge shall be taken as specified in Table 3.4.1-1 for live load surcharge.

$$h_{eq} = 2.00 \text{ ft}$$

$$\begin{aligned} \Delta &= 0.27 \text{ klf} = 0.27 \times 0.125 \text{ kcf} \times 2.00 \text{ ft} \times 4.00 \text{ ft} \\ Y &= 2.00 \text{ ft} = 4.00 \text{ ft} / 2 \\ H &= 0.25 \text{ klf} = 0.27 \text{ klf} \times 0.92 \\ V &= 0.11 \text{ klf} = 0.27 \text{ klf} \times 0.40 \\ X &= -3.00 \text{ ft} \end{aligned}$$

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For bearing evaluation, also include vertical component of live load surcharge.

$$P = 1.50 \text{ klf} = 0.125 \text{ kcf} \times 2.00 \text{ ft} \times 6.00 \text{ ft}$$

Vehicular Impact:

$$P = 23.0 \text{ k} \quad (\text{Ref I - Table 3.3.2-1, TL 2})$$

$$H = 2.00 \text{ ft} \quad (\text{Ref I - Table 3.3.2-1, TL 2})$$

$$L = 20.00 \text{ ft} \quad (\text{Ref I - 3.3.2.4, entire wall length can be used to resist impact})$$

$$P = 1.15 \text{ klf} = 23.0 \text{ k} / 20.00 \text{ ft}$$

$$Y = 6.00 \text{ ft} = 4.00 \text{ ft} + 2.00 \text{ ft}$$

Load Factors:

	Strength I		Extreme II
	Bearing	Sliding/Ecc.	
EV	1.35	1.00	1.00
EH	1.50	1.50	1.00
LS	1.75	1.75	0.50
CT	0.00	0.00	1.00

Strength I, Bearing Evaluation:

Loads:

	Unfactored	Load Factor	Factored	V or H
EV	3.00 klf	1.35	4.05 klf	V
EHh	0.25 klf	1.50	0.37 klf	H
EHv	0.11 klf	1.50	0.16 klf	V
LSH	0.25 klf	1.75	0.44 klf	H
LSv	0.11 klf	1.75	0.19 klf	V
LS-Vert	1.50 klf	1.75	2.63 klf	V
CT	1.15 klf	0.00	0.00 klf	H

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	H	Y	V	X	M
EV	0.00 klf	-	4.05 klf	0.00 ft	0.00 k-ft
EHh	0.37 klf	1.33 ft	0.00 klf	-	0.50 k-ft
EHv	-	-	0.16 klf	-3.00 ft	-0.48 k-ft
LSH	0.44 klf	2.00 ft	0.00 klf	-	0.87 k-ft
LSv	-	-	0.19 klf	-3.00 ft	-0.56 k-ft
LS-Vert	0.00 klf	-	2.63 klf	-	0.00 k-ft
CT	0.00 klf	6.00 ft	0.00 klf	-	0.00 k-ft
	<u>0.81 klf</u>		<u>7.02 klf</u>		<u>0.32 k-ft</u>

Eccentricity, $e = 0.05 \text{ ft} = 0.32 \text{ k-ft} / 7.02 \text{ klf}$

Effective Width, $B' = 5.91 \text{ ft} = 6.00 \text{ ft} - 2 \times 0.05 \text{ ft}$

Applied Pressure = $1.19 \text{ ksf} = 7.02 \text{ klf} / 5.91 \text{ ft}$

Ultimate Bearing Capacity = 6.67 ksf (see bearing capacity calculations, minimum from B-1/B-2 used)

Applied	<	Allowable
<u>1.19 ksf</u>	<	<u>6.67 ksf</u>

OK

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Strength I, Sliding and Eccentricity Evaluation:

Loads:

	Unfactored	Load Factor	Factored	V or H
EV	3.00 klf	1.00	3.00 klf	V
EHh	0.25 klf	1.50	0.37 klf	H
EHv	0.11 klf	1.50	0.16 klf	V
LSH	0.25 klf	1.75	0.44 klf	H
LSv	0.11 klf	1.75	0.19 klf	V
LS-Vert	1.50 klf	0.00	0.00 klf	V
CT	1.15 klf	0.00	0.00 klf	H

	H	Y	V	X	M
EV	0.00 klf	-	3.00 klf	0.00 ft	0.00 k-ft
EHh	0.37 klf	1.33 ft	0.00 klf	-	0.50 k-ft
EHv	-	-	0.16 klf	-3.00 ft	-0.48 k-ft
LSH	0.44 klf	2.00 ft	0.00 klf	-	0.87 k-ft
LSv	-	-	0.19 klf	-3.00 ft	-0.56 k-ft
LS-Vert	0.00 klf	-	0.00 klf	-	0.00 k-ft
CT	0.00 klf	6.00 ft	0.00 klf	-	0.00 k-ft
	<u>0.81 klf</u>		<u>3.35 klf</u>		<u>0.32 k-ft</u>

Eccentricity Check:

$$\text{Eccentricity, } e = 0.10 \text{ ft} = \frac{0.32 \text{ k-ft}}{3.35 \text{ klf}}$$

Per Ref 1 - 11.6.3.3, for foundations on soil, the location of the resultant of the reaction forces shall be within the middle two-thirds of the base width.

$$\text{Allowable } e = 2.00 \text{ ft} > 0.10 \text{ ft} \quad \text{OK}$$

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Sliding Check:

10.6.3.4—Failure by Sliding

Failure by sliding shall be investigated for footings that support horizontal or inclined load and/or are founded on slopes.

For foundations on clay soils, the possible presence of a shrinkage gap between the soil and the foundation shall be considered. If passive resistance is included as part of the shear resistance required for resisting sliding, consideration shall also be given to possible future removal of the soil in front of the foundation.

The factored resistance against failure by sliding, in kips, shall be taken as:

$$R_R = \phi R_u = \phi_i R_i + \phi_{ep} R_{ep} \quad (10.6.3.4-1)$$

where:

- ϕ = resistance factor (dim)
- R_u = nominal sliding resistance against failure by sliding (kips)
- ϕ_i = resistance factor for shear resistance between soil and foundation specified in Table 10.5.5.2.2-1
- R_i = nominal sliding resistance between soil and foundation (kips)
- ϕ_{ep} = resistance factor for passive resistance specified in Table 10.5.5.2.2-1
- R_{ep} = nominal passive resistance of soil available throughout the design life of the structure (kips)

If the soil beneath the footing is cohesionless, the nominal sliding resistance between soil and foundation shall be taken as:

$$R_i = CV \tan \phi_f \quad (10.6.3.4-2)$$

for which:

- C = 1.0 for concrete cast against soil
- = 0.8 for precast concrete footing

where:

- ϕ_f = internal friction angle of drained soil (degrees)
- V = total vertical force (kips)

$$\text{Min. } \phi = 35.00 \text{ deg}$$

$$\tan(\phi) = 0.70$$

$$C = 1$$

$$V = 3.35 \text{ klf}$$

$$R = 2.34 \text{ klf} = 1 \times 3.35 \text{ klf} \times 0.70$$

$$\phi = 0.9 \quad (\text{Ref 1 - Table 10.5.5.2.2-1, soil on soil})$$

$$\phi R_n = 2.11 \text{ klf} = 0.90 \times 2.34 \text{ klf}$$

$$\text{Applied H} = 0.81 \text{ klf} < 2.11 \text{ klf} \quad \text{OK}$$

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Extreme 2 Evaluation:

Loads:

	Unfactored	Load Factor	Factored	V or H
EV	3.00 klf	1.00	3.00 klf	V
EHh	0.25 klf	1.00	0.25 klf	H
EHv	0.11 klf	1.00	0.11 klf	V
LSH	0.25 klf	0.50	0.12 klf	H
LSv	0.11 klf	0.50	0.05 klf	V
LS-Vert	1.50 klf	0.00	0.00 klf	V
CT	1.15 klf	1.00	1.15 klf	H

	H	Y	V	X	M
EV	0.00 klf	-	3.00 klf	0.00 ft	0.00 k-ft
EHh	0.25 klf	1.33 ft	0.00 klf	-	0.33 k-ft
EHv	-	-	0.11 klf	-3.00 ft	-0.32 k-ft
LSH	0.12 klf	2.00 ft	0.00 klf	-	0.25 k-ft
LSv	-	-	0.05 klf	-3.00 ft	-0.16 k-ft
LS-Vert	0.00 klf	-	0.00 klf	-	0.00 k-ft
CT	1.15 klf	6.00 ft	0.00 klf	-	6.90 k-ft
	<u>1.52 klf</u>		<u>3.16 klf</u>		<u>7.00 k-ft</u>

Eccentricity Check:

$$\text{Eccentricity, } e = 2.21 \text{ ft} = \frac{7.00 \text{ k-ft}}{3.16 \text{ klf}}$$

Per Ref 1 - 11.6.5.1, for foundations on soil and rock, the location of the resultant of the reaction forces shall be within the middle eight-tenths of the base width for Extreme Event.

$$\text{Allowable } e = 2.40 \text{ ft} > 2.21 \text{ ft} \quad \text{OK}$$

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Sliding Check:

$$\text{Min. } \phi = 35.00 \text{ deg}$$

$$\tan(\phi) = 0.70$$

$$C = 1$$

$$V = 3.16 \text{ klf}$$

$$R = 2.21 \text{ klf} = 1 \times 3.16 \text{ klf} \times 0.70$$

$$\phi = 1 \text{ (Ref 1 - Extreme Event)}$$

$$\phi R_n = 2.21 \text{ klf} = 1.00 \times 2.21 \text{ klf}$$

$$\text{Applied H} = 1.52 \text{ klf} < 2.21 \text{ klf} \quad \text{OK}$$

APPENDIX

6.7. Preliminary Plans

